Tuesday, September 26, 2017

75. 6 revolutions per second

$$= \frac{6 \text{ revolutions}}{1 \text{ second}} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolutions}} = \frac{12\pi \text{ radians}}{1 \text{ seconds}}$$
$$= \frac{12\pi \text{ radians per second}}{1 \text{ radians per second}}$$

76. 20 revolutions per second

$$= \frac{20 \text{ revolutions}}{1 \text{ second}} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}} = \frac{40\pi \text{ radians}}{1 \text{ second}}$$
$$= \frac{40\pi \text{ radians per second}}{1 \text{ revolution}} = \frac{40\pi \text{ radians}}{1 \text{ second}}$$

92. The distance that the wheel moves is given by $s = r\theta$. We are given that r = 80 centimeters and $\theta = 60^{\circ}$. The formula $s = r\theta$ can only be used when θ is expressed in radians.

$$60^{\circ} = 60^{\circ} \cdot \frac{\pi \text{ radians}}{180^{\circ}} = \frac{60\pi}{180} \text{ radians}$$
$$= \frac{\pi}{3} \text{ radians}$$

The length that the wheel moves is

$$s = r\theta = (80 \text{ centimeters}) \left(\frac{\pi}{3}\right) = \frac{80\pi}{3} \text{ centimeters}$$

 \approx 83.78 centimeters.

98. Linear speed is given by $v = r\omega$. We are given that r = 25 feet and the wheel rotates at 3 revolutions per minute. We need to convert 3 revolutions per minute to radians per minute.

3 revolutions per minute

= 3 revolutions per minute
$$\cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}}$$

 $=6\pi$ radians per minute

$$v = r\omega = (25 \text{ feet})(6\pi) \approx 471 \text{ feet per minute}$$

The linear speed of the Ferris wheel is about 471 feet per minute.

90. The distance that the tip of the minute hand moves is given by its arc length, s. Since $s = r\theta$, we begin by finding r and θ . We are given that

r = 6 inches. The minute hand moves from 12 to 4

o'clock, or $\frac{1}{3}$ of a complete revolution. The formula

 $s = r\theta$ can only be used when θ is expressed in

radians. We must convert $\frac{1}{3}$ revolution to radians.

$$\frac{1}{3} \text{ revolution} = \frac{1}{3} \text{ revolution} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}}$$
$$= \frac{2\pi}{3} \text{ radians}$$

The distance the tip of the minute hand moves is

$$s = r\theta = (6 \text{ inches}) \left(\frac{2\pi}{3}\right) = \frac{12\pi}{3} \text{ inches}$$

 $=4\pi$ inches ≈ 12.57 inches.

97. Linear speed is given by $v = r\omega$. We are given that

$$\omega = \frac{\pi}{12}$$
 radians per hour and

$$r = 4000$$
 miles. Therefore,

$$v = r\omega = (4000 \text{ miles}) \left(\frac{\pi}{12}\right)$$

$$= \frac{4000\pi}{12}$$
 miles per hour

The linear speed is about 1047 miles per hour.

99. Linear speed is given by $v = r\omega$. We are given that r = 12 feet and the wheel rotates at 20 revolutions per minute.

20 revolutions per minute

= 20 revolutions per minute
$$\cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}}$$

=
$$40\pi$$
 radians per minute

$$v = r\omega = (12 \text{ feet})(40\pi)$$

The linear speed of the wheel is about 1508 feet per minute.

100. Begin by converting 2.5 revolutions per minute to radians per minute.

2.5 revolutions per minute

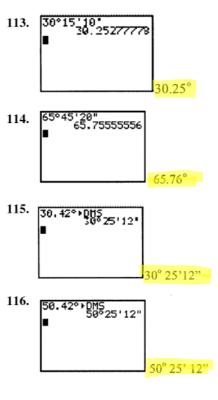
= 2.5 revolutions per minute $\frac{2\pi \text{ radians}}{1 \text{ revolution}}$

 $=5\pi$ radians per minute

The linear speed of the animals in the outer rows is $v = r\omega = (20 \text{ feet})(5\pi) \approx 100 \text{ feet per minute}$

The linear speed of the animals in the inner rows is $v = r\omega = (10 \text{ feet})(5\pi) \approx 50 \text{ feet per minute}$

The difference is $100\pi - 50\pi = 50\pi$ feet per minute or about 157.08 feet per minute.



Screen clipping taken: 9/29/2017 8:43 AM