# **UNIT 10 – Circles NOTES**

Name:

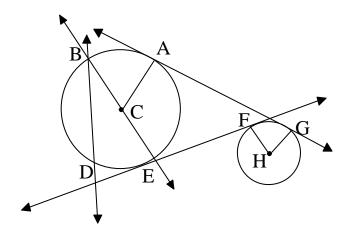
# **Day 1 Circle Basics**

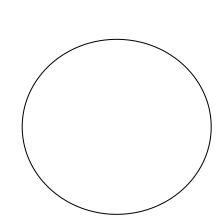
**Objectives: SWBAT** identify segments and lines related to circles. **SWBAT** Use properties of a tangent to a circle.

- A. Definitions in Circles
  - 1. Circle
  - 2. Radius
  - 2. Diameter
  - 3. Chord
  - 4. Interior of a Circle
  - 5. Exterior of a Circle
  - 6. On the Circle

#### Use the diagram to find the following segments (name all).

- 1. Chords
- 2. Diameters
- 4. Radii
- 5. Center of a Circle



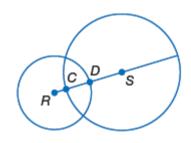


## **Diameter of a Circle Formula**

#### **Examples:**

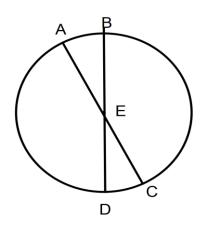
Use the diagrams to find the following.

1. The diameter of  $\bigcirc S$  is 30 cm. The diameter of  $\bigcirc R$  is 20 cm. DS = 9 Find the length of CD.



#### All Radii the same circle are \_\_\_\_\_

2. Given: DB = 13 units long Find the length of EC.



Area of a Circle Formula

**Circumference of a Circle Formula** 

The \_\_\_\_\_\_ is the common variable in <u>all three</u> of the above formulas.

Find the following.

- 3. A circle has a radius of 3ft. What's the diameter?
- 4. A circle has a diameter of 5in. What's the radius?

- 5. If a circle has a diameter of 6ft. What's the Circumference?
- 6. What is the area of a circle if the circumference is  $20\pi in$ ?
- 7. Using a string a student decided to determine the diameter of a large trash can. If the string 60 inches long will wrap around the trash can, what is approximate diameter of the trash can?

## **Day 2 Central Angles and Arcs**

**Objectives: SWBAT** use properties of arcs of circles. **SWBAT** use properties of chords of circles.

360 Degree Theorem -

Central Angle -

Arc –

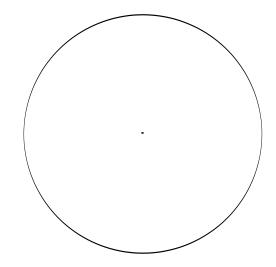
Minor Arc -

Major Arc -

Semicircle –

**Central Angle – Arc Theorem** 

When reading an arc and finding the measurements of arcs, you should always use the \_\_\_\_\_ path.



## **Examples:**

 $\overline{MQ}$  and  $\overline{NR}\,$  are diameters. Find the indicated measure.

<b>1.</b> m <i>MN</i>	<b>2.</b> mNQ	M
<b>3.</b> mNQR	<b>4.</b> mMRP	N 70° O 30°
<b>5.</b> mQR	<b>6.</b> mMR	P

Q

R

# Arc Length Formula

## Find the length of the following arcs.

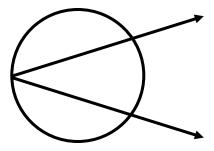
7.	ÛR	<b>8.</b> <i>RS</i>	R
9.	STU	<b>10.</b> <i>RT</i>	U 60° U 4 ft
11.	ŨRS	<b>12.</b> <i>ST</i>	T

## **Day 3 Inscribed Angles**

**Objectives: SWBAT** use inscribed angles to solve problems. **SWBAT** use properties of inscribed polygons.

**Inscribed angle:** 

**Intercepted Arc:** 

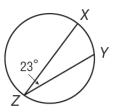


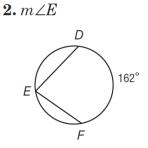
## **Measure of Inscribed Angle**

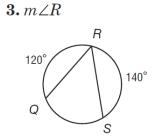
## **Examples:**

Find the measure of the indicated arc or angle in  $\Box O$ .

**1.**  $m \widehat{XY}$ 

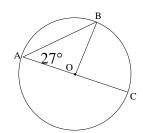




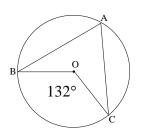


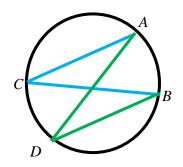




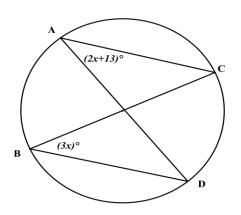


**Two Inscribed Angles Theorem** 

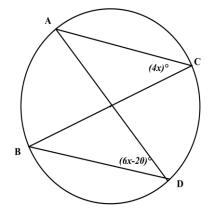




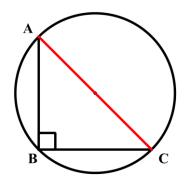
**7.** Find *x* 

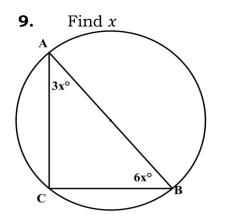


**8.** Find  $\widehat{mAB}$ 

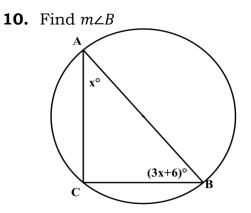


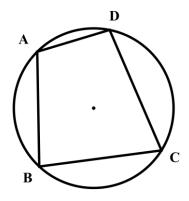
# **Inscribed Right Triangle Theorem**



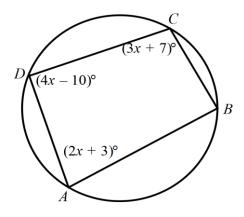


# **Inscribed Quadrilateral Theorem**





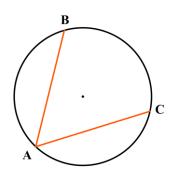
#### **11.** Find the value of *x*



## **Day 4 Chords and Arcs**

**Objectives: SWBAT** use properties of arcs of circles. **SWBAT** use properties of chords of circles.

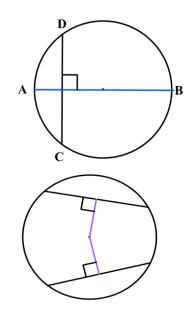
1. Chord – Arc Theorem



2. Perpendicular Bisector of a Circle Theorem

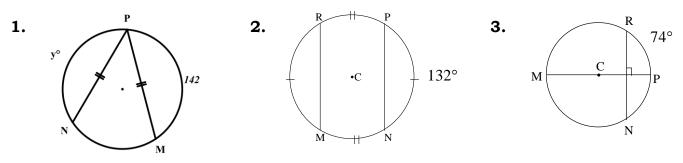
Converse

3. Equidistant Chord Theorem

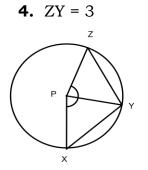


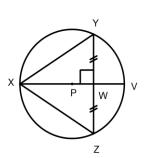
## **Examples:**

Find the measure of  $\widehat{MN}$ .

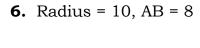


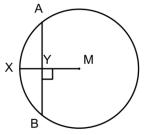
#### <u>P is the center of the circle.</u> Use the given information to find XY.



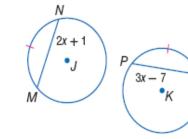


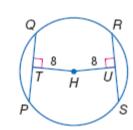
**5.** ZY = 6, XW = 4





**7.** ALGEBRA In the figures,  $\bigcirc J \cong \bigcirc K$  and  $\widehat{MN} \cong \widehat{PQ}$ . Find PQ.





Q

8.

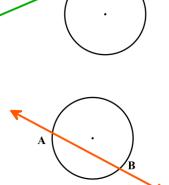
In  $\bigcirc H$ , PQ = 3x - 4 and RS = 14. Find x.

# **Day 5 Tangents of Circles**

**Objectives: SWBAT** identify segments and lines related to circles. **SWBAT** Use properties of a tangent to a circle.

# Tangent



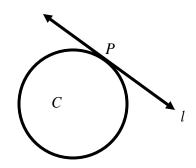


B

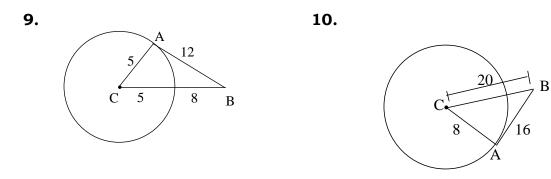
## **Examples:**

1. F	A. Center
2. $\overrightarrow{FE}$	B. Chord
3. $\overline{HG}$	C. Diameter B A
4. $\overline{DB}$	D. Radius
5. C	E. Point of Tangency
6. $\overline{BE}$	F. Common External Tangent
7. $\overrightarrow{DB}$	G. Common Internal Tangent DE
8. $\overrightarrow{AG}$	H. Secant

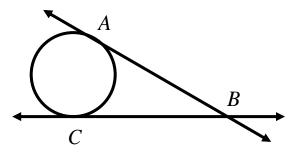
# **Perpendicular Tangent Theorem**



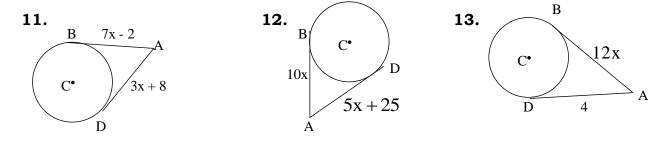
#### Tell whether $\overrightarrow{AB}$ is tangent to $\bigcirc C$ . Explain you reasoning



## **Intersecting Tangent Theorem**

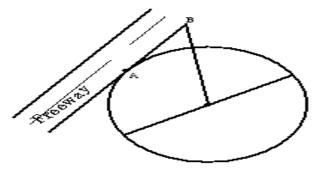


### **Examples:**



#### 14.

A freeway runs tangent to a circular lake. The distance from point B to the center of the lake is 100 miles. The distance from Point A to Point B on the freeway is 80 miles. What is the diameter of the lake?

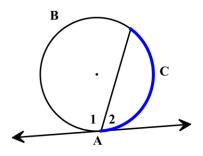


# **Day 6 Angle Relationships in Circles**

**Objectives: SWBAT** use angles formed by tangents and chords to solve problems. **SWBAT** use angles formed by lines that intersect a circle to solve problems.

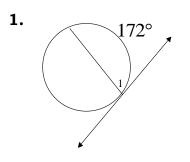
2.

## Intersecting a Tangent and a Chord

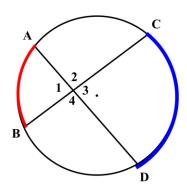


#### **Examples:**

Find the measure of  $\angle 1$ .



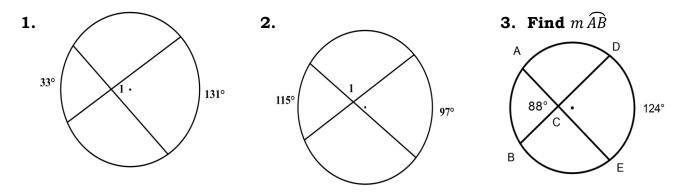
# 128°



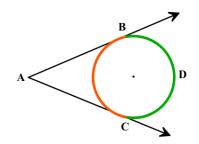
## **Interior intersection of two Chords**

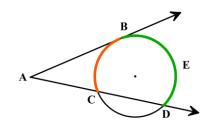
## **Examples:**

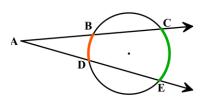
Find the measure of  $\angle 1$ .

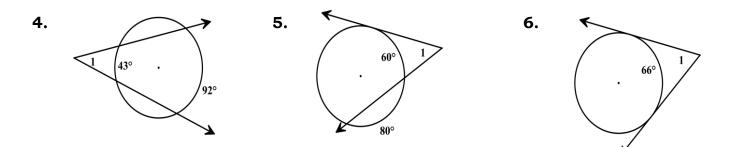


# **Exterior Intersection**







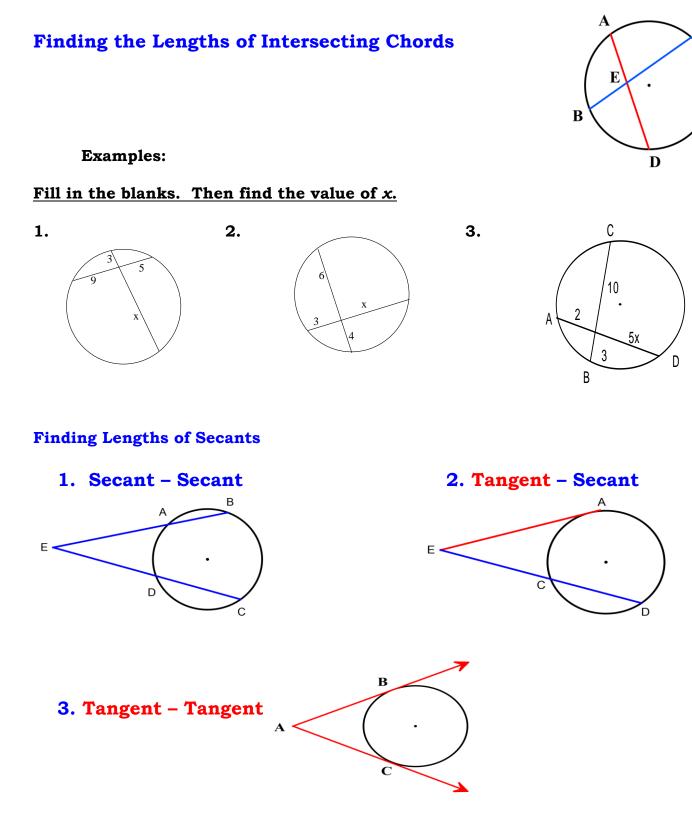


Angle Location		Angle – Arc Relationship	
Where is the vertex of my angle?	Angle Name		
CENTER			
ON			
INSIDE (Not Center)			
OUTSIDE			

# **Day 7 Segment Lengths in Circles**

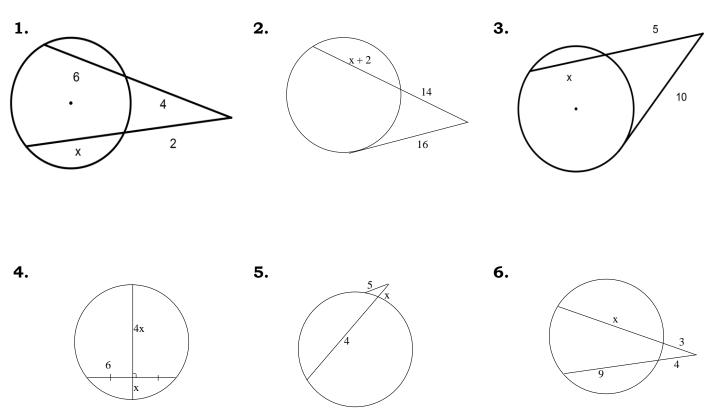
**Objectives: SWBAT** find the lengths of segments of chords. **SWBAT** find the lengths of segments of tangents and secants.

С



# Examples:

Find the value of x.



**Review of Factoring** 

X Method

$$\frac{-b\pm\sqrt{b^2-4ac}}{2a}$$

Secant - Secant	Tangent - Secant	Chord - Chord	Tangent - Tangent

## **Day 8 Equations of Circles**

**Objectives: SWBAT** write the equation of a circle. **SWBAT** use the equation of a circle and its graph to solve problems.

#### **Standard Equation of Circle**

### **Examples:**

Match the equation of a circle with its description.

1.  $(x+2)^2 + (y-3)^2 = 4$ a. Center (-3, 5), radius 42.  $(x-2)^2 + (y-5)^2 = 4$ b. Center (-2, -3), radius 23.  $(x+3)^2 + (y-5)^2 = 16$ c. Center (-2, 3), radius 24.  $(x+2)^2 + (y+3)^2 = 4$ d. Center (2, -5), radius 25.  $(x+3)^2 + (y+5)^2 = 16$ e. Center (-3, -5), radius 46.  $(x-2)^2 + (y+5)^2 = 4$ f. Center (2, 5), radius 2

Give the center and the radius of each circle.

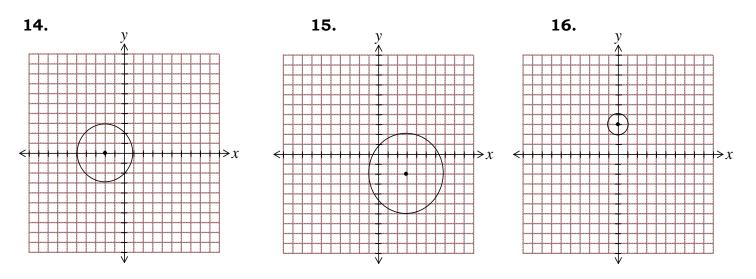
- **7.**  $(x-4)^2 + (y+2)^2 = 25$ **8.**  $(x+2)^2 + (y+4)^2 = 9$
- **9.**  $(x-5)^2 + (y-3)^2 = 16$ **10.**  $(x+6)^2 + (y-4)^2 = 4$

Write the standard equation of the circle with the given center and radius.**11.** center (0,4), radius 512. center (-3, 6), radius 7

**13.** center (0,0), radius 1

# **Graphing Circles**

Give the coordinates of the center, the radius and the equation of the circle.



Graph the circle given the equation.

4. 
$$(x+4)^2 + (y-2)^2 = 9$$

5.  $(x-5)^2 + y^2 = 4$ 

