

Trig 4.5 – Worksheet Intro to Graphing $\sin(x)$ and $\cos(x)$

Name _____

Graph each on the grid provided.

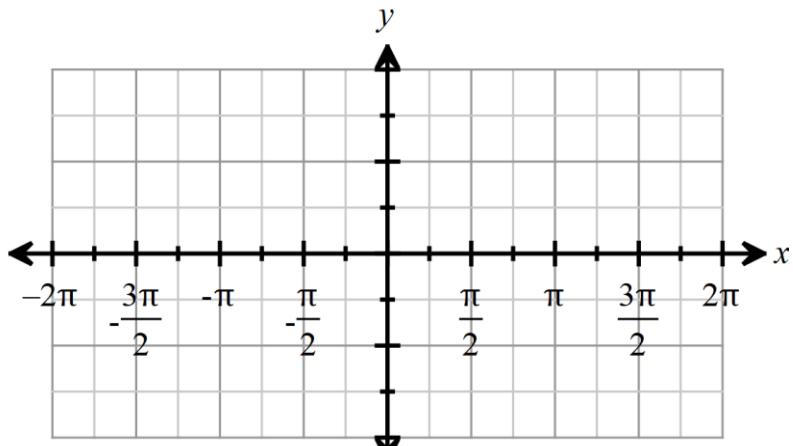
1) $y = -2\cos(x)$

A = _____

P = _____

D: _____

R: _____



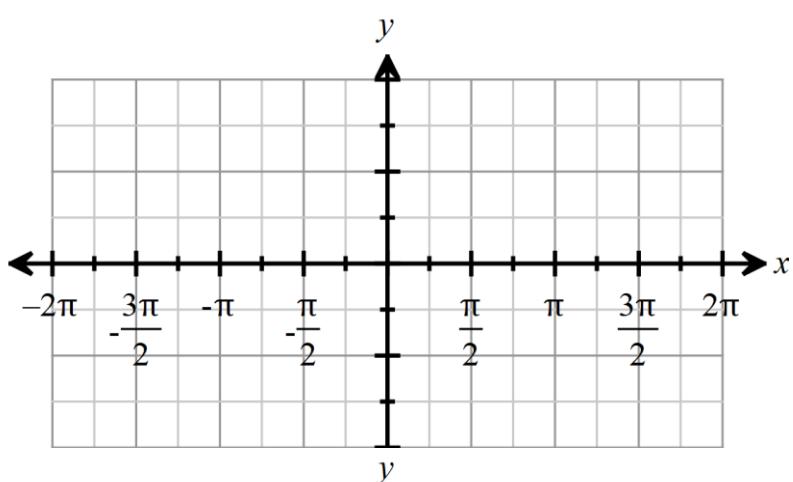
2) $y = -3\sin(x) + 1$

A = _____

P = _____

D: _____

R: _____



3) $y = 2\sin\left(x - \frac{\pi}{2}\right)$

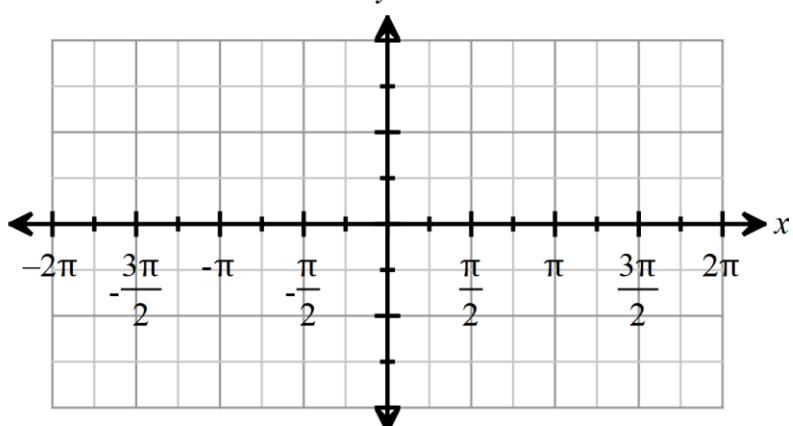
A = _____

P = _____

D: _____

R: _____

P.S. _____



4) $y = 3\cos(x - \pi)$

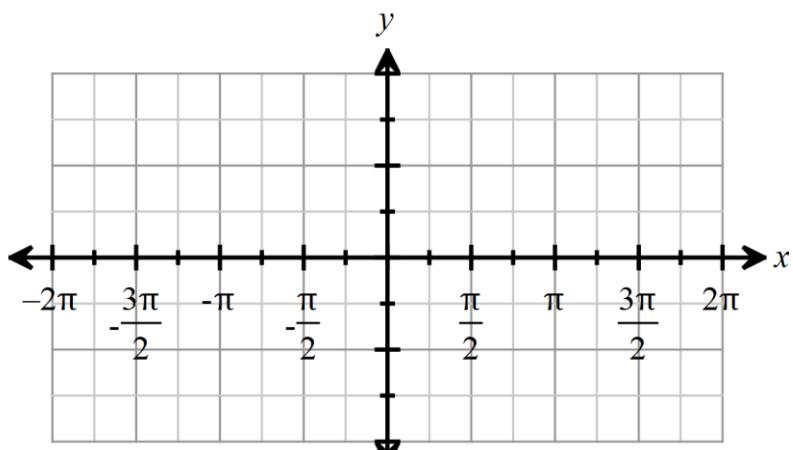
A = _____

P = _____

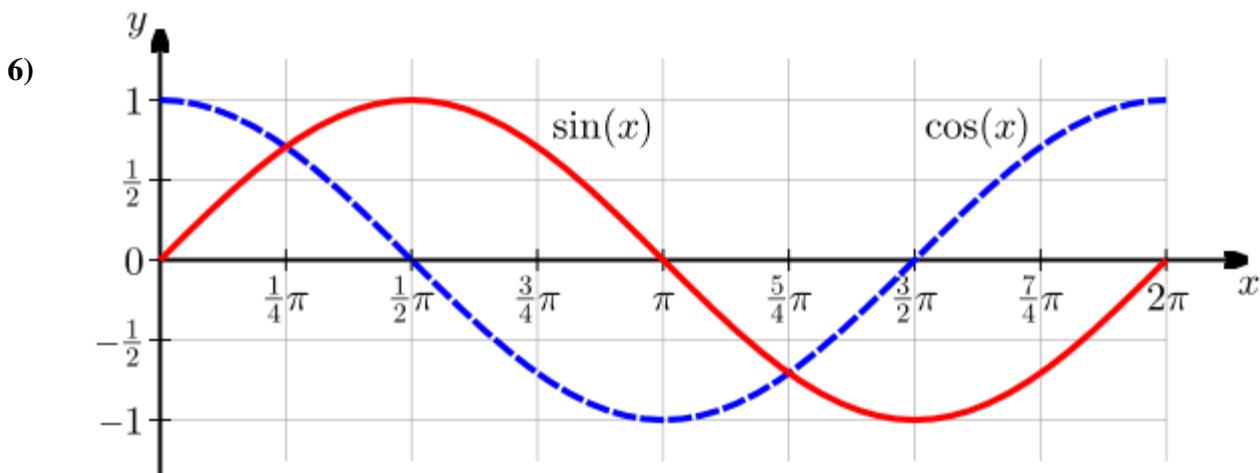
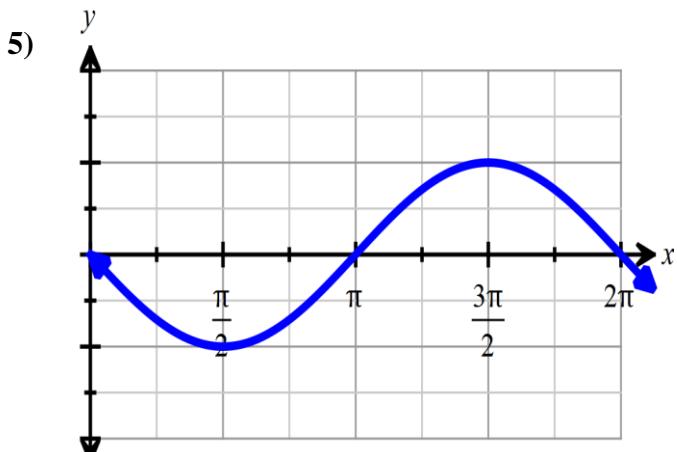
D: _____

R: _____

P.S. _____



Write an equation for the given graph.



Analyze the $\cos(x)$ and $\sin(x)$ graphs above and use a phase shift to write $\sin(x)$ in terms of $\cos(x)$...

$$\sin(x) = \underline{\hspace{2cm}}$$

Then do the same for $\cos(x)$...

$$\cos(x) = \underline{\hspace{2cm}}$$

Find the amplitude, phase shift, and vertical shift of each.

7) $y = 2\sin\left(x - \frac{\pi}{4}\right) + 2$

8) $y = -7\cos\left(x + \frac{\pi}{9}\right) - 4$

9) $y = 1.6\sin(x + 5\pi) + 3$

Trig 4.5A Worksheet – Graphing $\sin(x)$ and $\cos(x)$
Compressions and Stretches

Graph each on the grid provided.

1) $y = -2\cos(2x)$

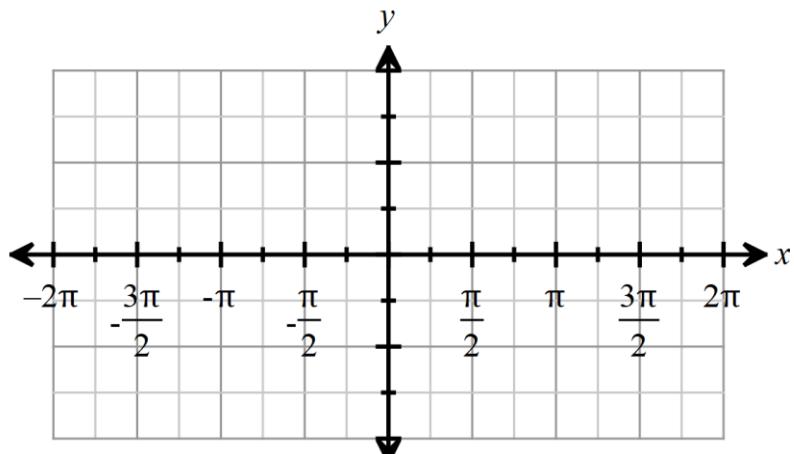
A = _____

P = _____

D: _____

R: _____

GAP: _____



2) $y = -3\sin(0.5x) + 1$

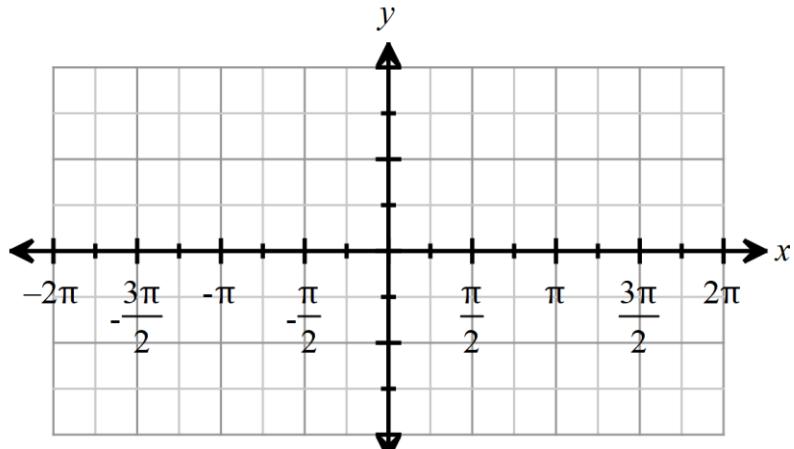
A = _____

P = _____

D: _____

R: _____

GAP: _____



3) $y = 2\sin(4x)$

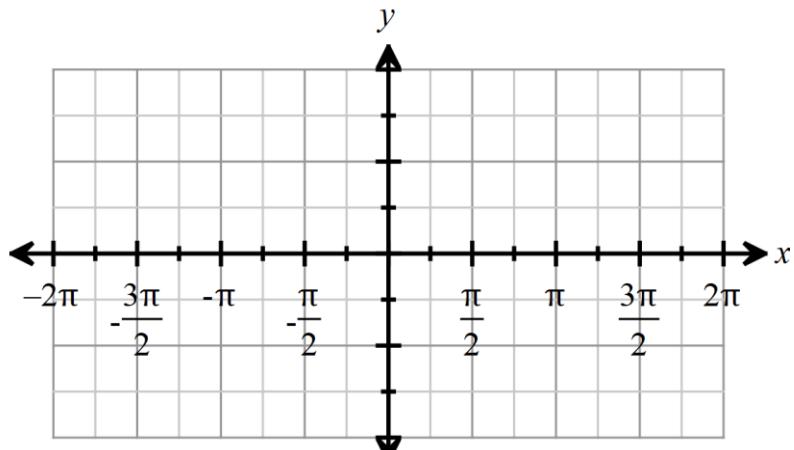
A = _____

P = _____

D: _____

R: _____

GAP: _____



4) $y = 3\cos\left(\frac{x}{3}\right) - 1$

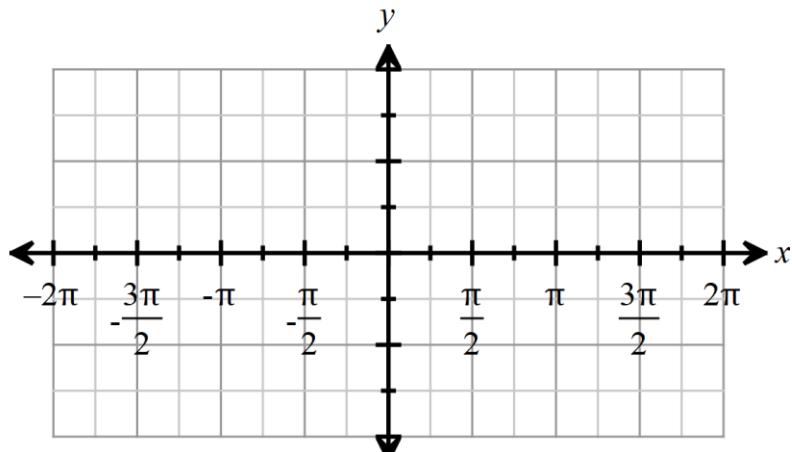
A = _____

P = _____

D: _____

R: _____

GAP: _____



5) $y = 2\sin(\pi x)$

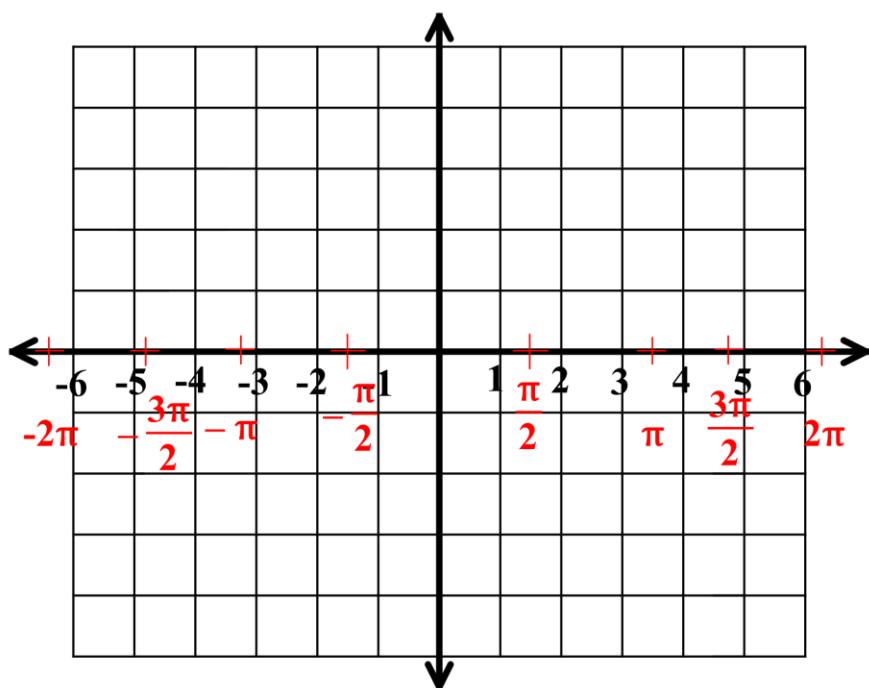
A = _____

P = _____

D: _____

R: _____

GAP: _____



Find the period of each.

6) $y = -4\cos(0.2x)$

7) $y = -16\sin 2\left(x - \frac{\pi}{9}\right)$

8) $y = 7\cos(3x - \pi)$

9) Write an equation of a sine function with amplitude 4, a range of [0,8] and a period of 4π .

10) Write an equation of a cosine function with amplitude 7, a range of [-8,6] and a period of $\frac{\pi}{6}$

Trig 4.5B Worksheet – Graphing $\sin(x)$ and $\cos(x)$ Compressions, Stretches, and Vertical Shifts

Graph each on the grid provided.

1) $y = -\cos(2x) + 1$

A = _____

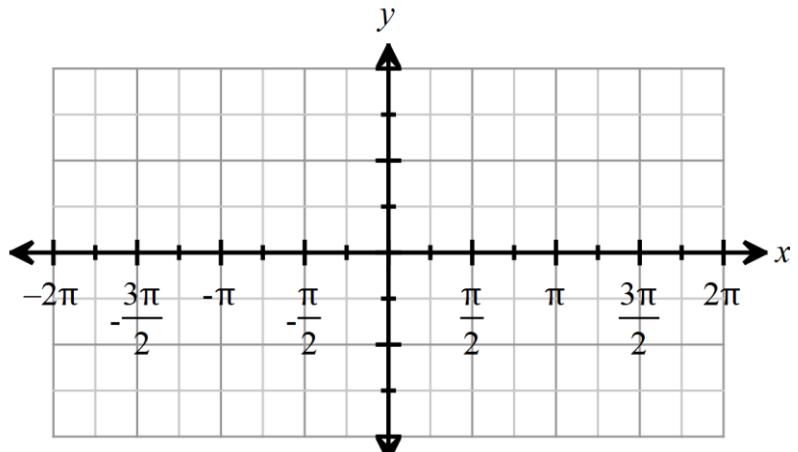
P = _____

D: _____

R: _____

Midline: _____

GAP: _____



2) $y = -\sin(0.5\pi x) - 1$

A = _____

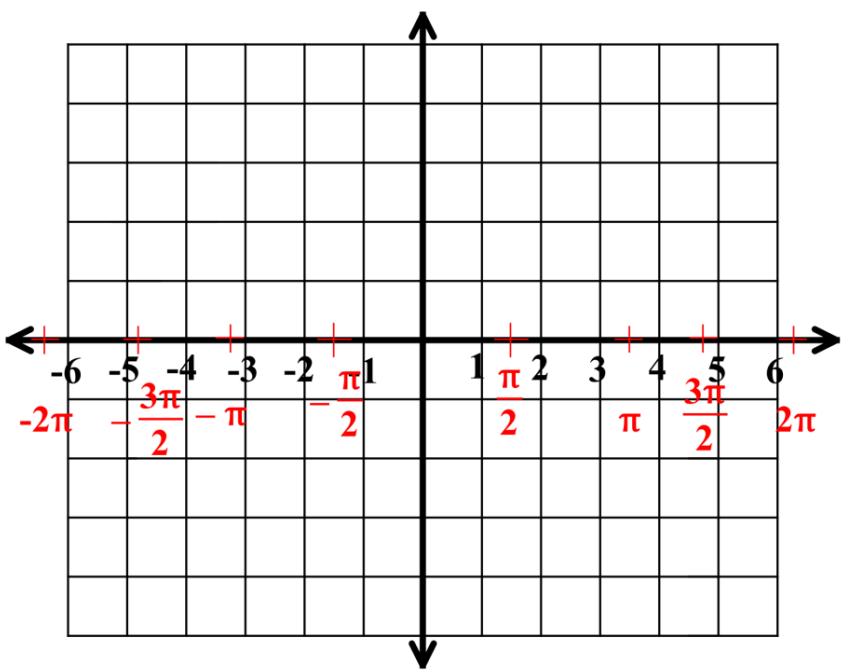
P = _____

D: _____

R: _____

Midline: _____

GAP: _____



3) $y = 2\sin 3(x) - 2$

A = _____

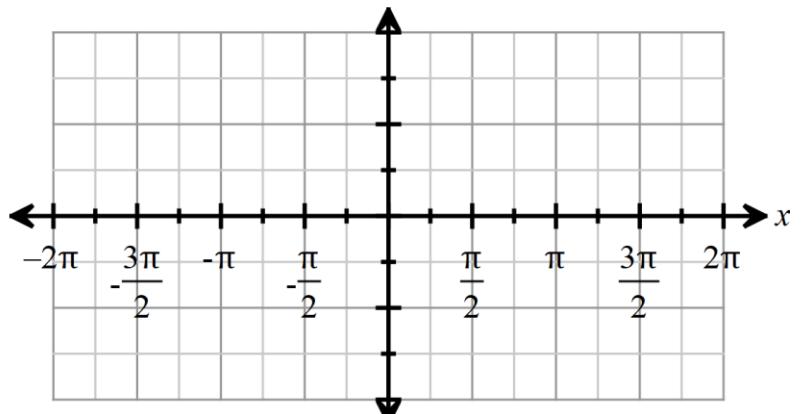
P = _____

D: _____

R: _____

Midline: _____

GAP: _____



4) $y = -2\sin\left(\frac{\pi}{3}x\right)$

A = _____

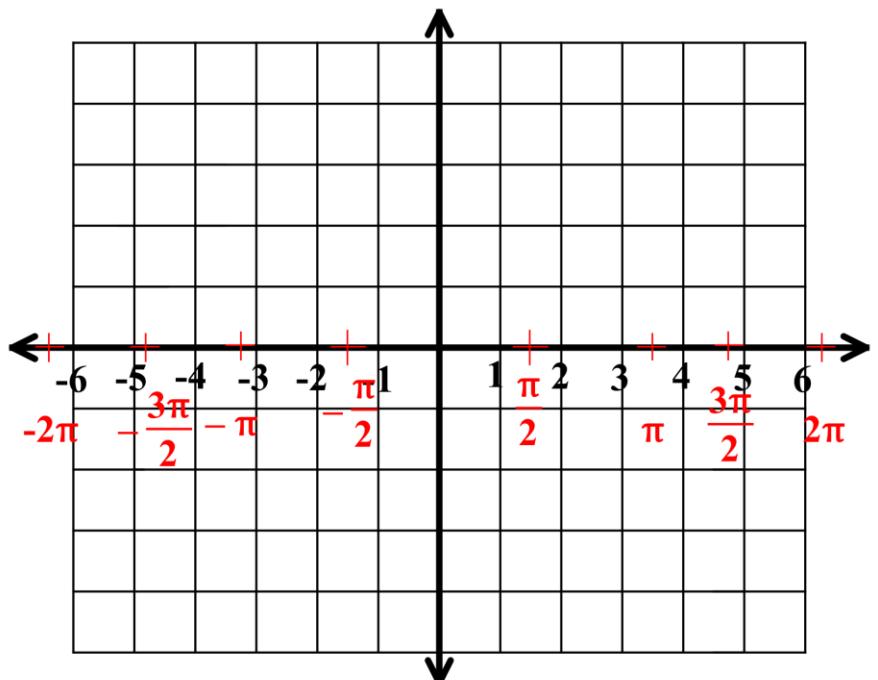
P = _____

D: _____

R: _____

Midline: _____

GAP: _____



Find the period and write an equation for the midline of each.

5) $y = -4\cos(0.1x) + 2$

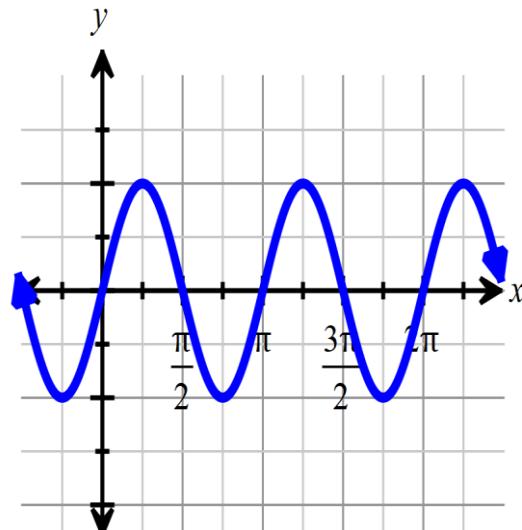
6) $y = -14\sin\left(4x - \frac{\pi}{9}\right) - 12$

7) $y = 7\cos(5x + \pi) + 10$

8) Write an equation of a sine function with amplitude 3, a range of [0,6] and a period of 8.

9) Write an equation of a cosine function with amplitude 12, a range of [-14, 10] and a period of $\frac{\pi}{8}$

10) Write an equation for the following graph as a sine and cosine function. .



Trig 4.5C Worksheet – Graphing $\sin(x)$ and $\cos(x)$ Compressions, Stretches, and Vertical Shifts

Graph each on the grid provided. The domain of all $\sin(x)$ and $\cos(x)$ graphs is all real numbers so I took that off.

1) $y = -\cos(2x - \pi)$

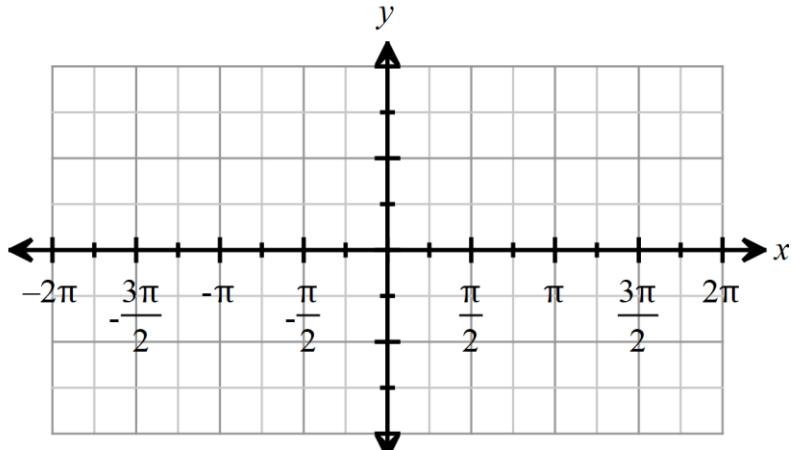
A = _____

P = _____

Phase Shift: _____

R: _____

GAP: _____



2) $y = 2\sin(0.5\pi x + \pi)$

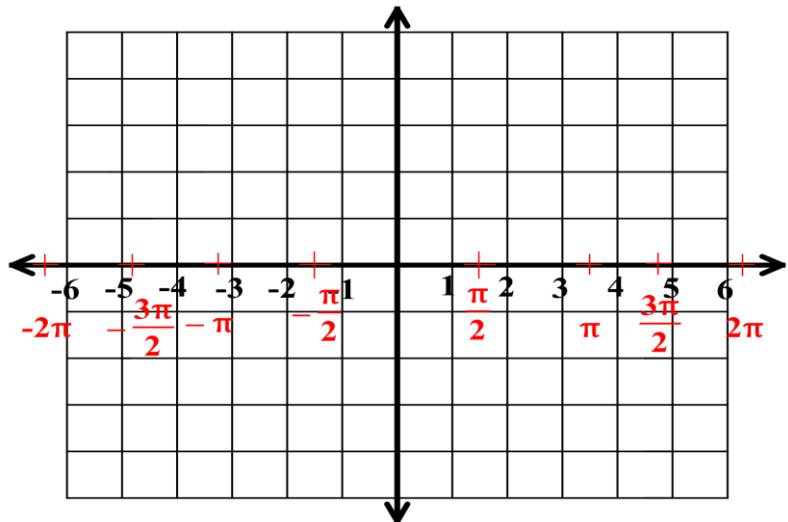
A = _____

P = _____

Phase Shift: _____

R: _____

GAP: _____



3) $y = -4\sin 3\left(x + \frac{\pi}{6}\right)$

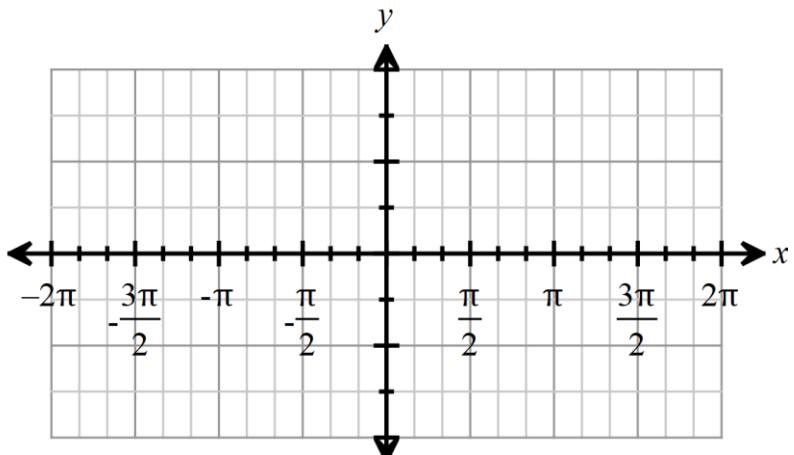
A = _____

P = _____

Phase Shift: _____

R: _____

GAP: _____



**Use the scale of $\frac{\pi}{6}$ **

4) $y = 2\cos(\pi x - 4\pi) + 1$

A = _____

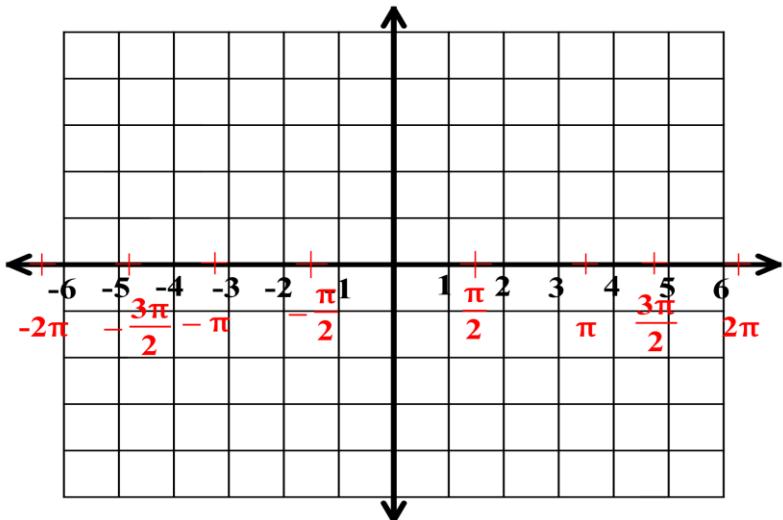
P = _____

Phase Shift: _____

R: _____

GAP: _____

Midline: _____



Find the period and phase shift.

5) $y = -4\cos(0.2x - 1) + 2$

6) $y = -14\sin 2 \left(x - \frac{\pi}{9} \right)$

7) $y = 7\cos(0.5x + \pi)$

8) Write an equation of a sine function with amplitude 7, a range of $[10, 24]$ and a period of 8π .

9) Write an equation of a cosine function with amplitude 13, a range of $[-13, 13]$ and a period of $\frac{\pi}{13}$

10) Find the value of k that will produce a phase shift of $\frac{2\pi}{7}$ given $y = 14\cos(3x - k)$.

11) What is the **maximum** value of the function $f(x) = 12\cos(4x) + 19$?

12) What is the **minimum** value of the function $f(x) = -15\sin(2x + \pi) - 20$?

Trig 4.6 Worksheet – Graphing $csc(x)$ and $sec(x)$

Graph each on the grid provided.

1) $y = -\sec(2x) + 1$

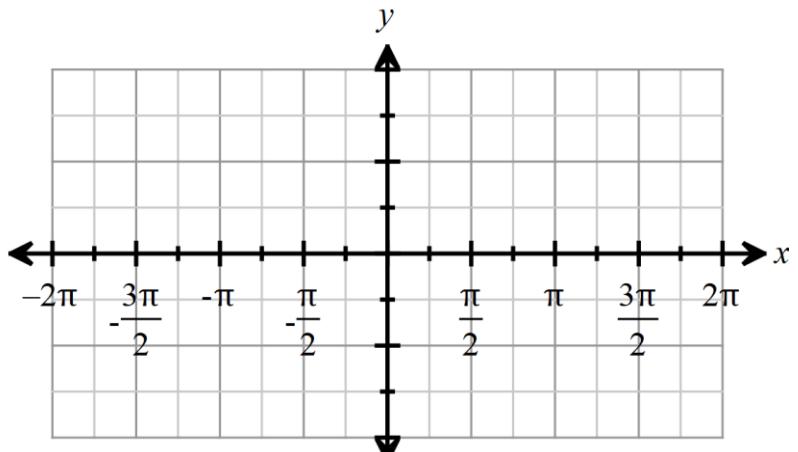
P = _____

D = _____

R: _____

VS: _____

GAP: _____



2) $y = -csc(0.5\pi x)$

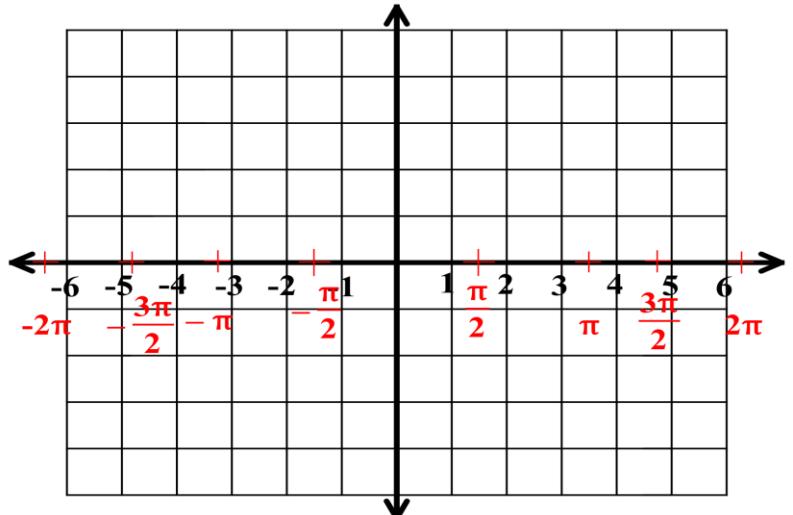
P = _____

D = _____

R: _____

VS: _____

GAP: _____



3) $y = 2csc3\left(x + \frac{\pi}{6}\right)$

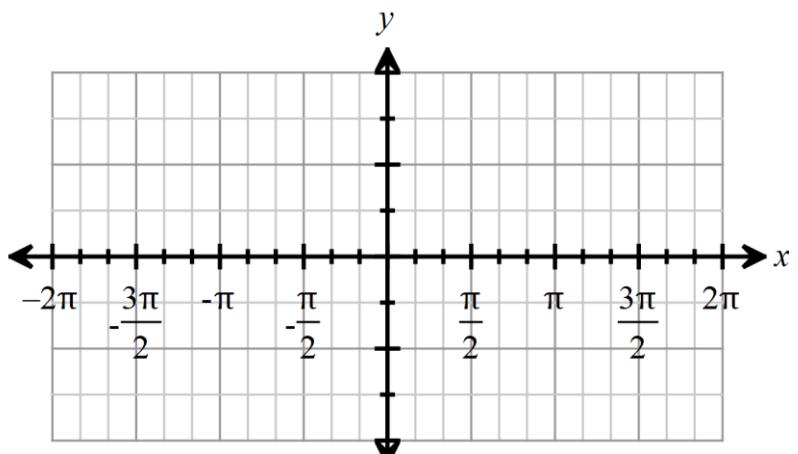
P = _____

D = _____

R: _____

VS: _____

GAP: _____



**Use the scale of $\frac{\pi}{6}$ **

4) $y = -2\sec\left(\frac{\pi}{3}x\right) + 1$

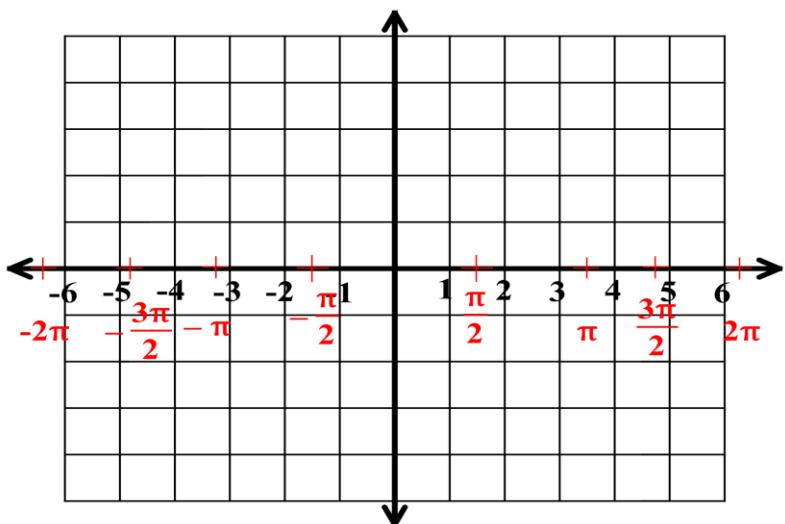
P = _____

D = _____

R: _____

VS: _____

GAP: _____



Find the range and phase shift for each.

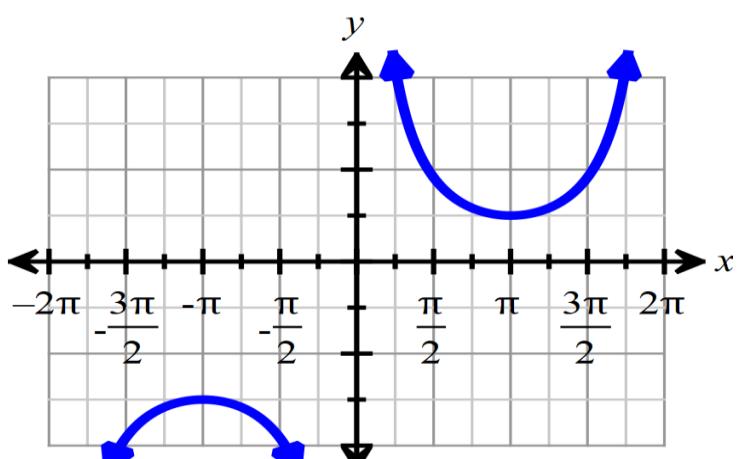
5) $y = -4\sec(.1x - \pi) + 2$

6) $y = -14\csc 4\left(x - \frac{\pi}{9}\right) - 14$

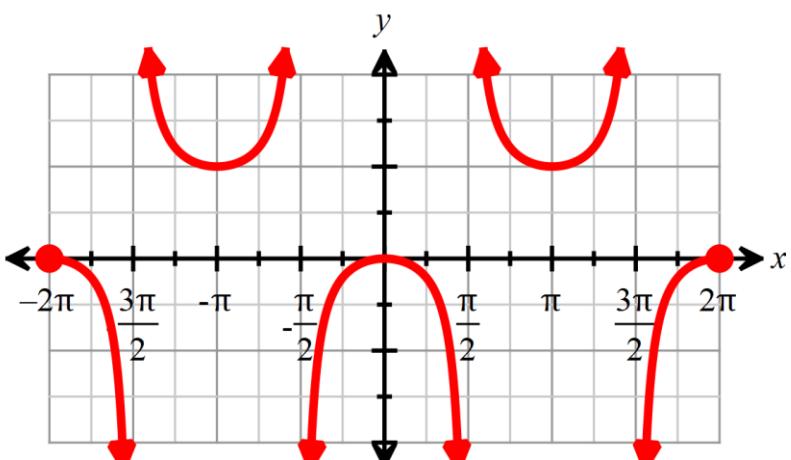
7) $y = 7\sec(5x + \pi) + 10$

Write equations for the following graphs.

8)



9)



Trig 4.6A Worksheet – Graphing $\tan(x)$ and $\cot(x)$

Graph the following functions. Please use a different color for each function.

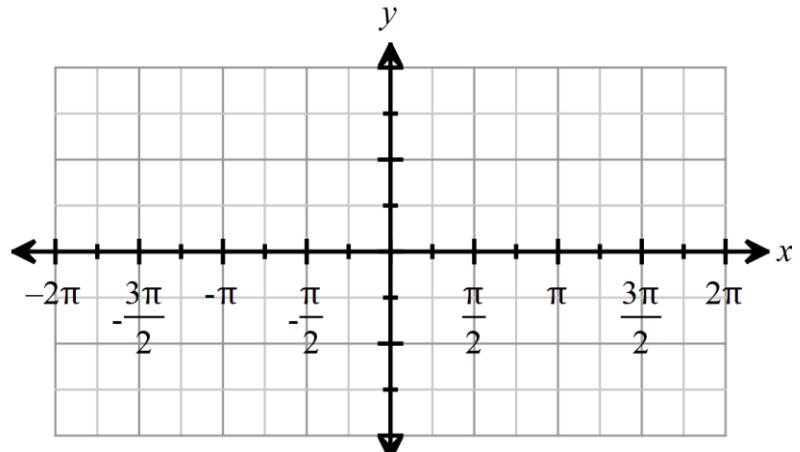
1) $y = 2\tan(x)$ and $y = -2\tan(x)$

P = _____

D = _____

R: _____

GAP: _____



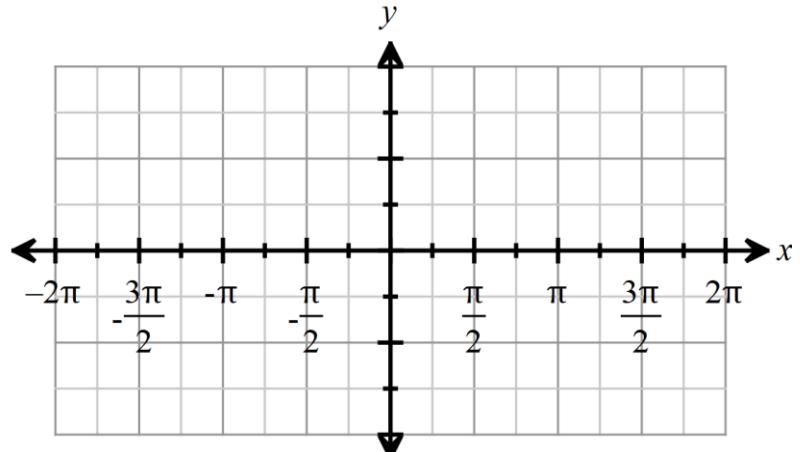
2) $y = 3\cot(x)$ and $y = -3\cot(x)$

P = _____

D = _____

R: _____

GAP: _____



3) $y = -\tan(x + \pi)$

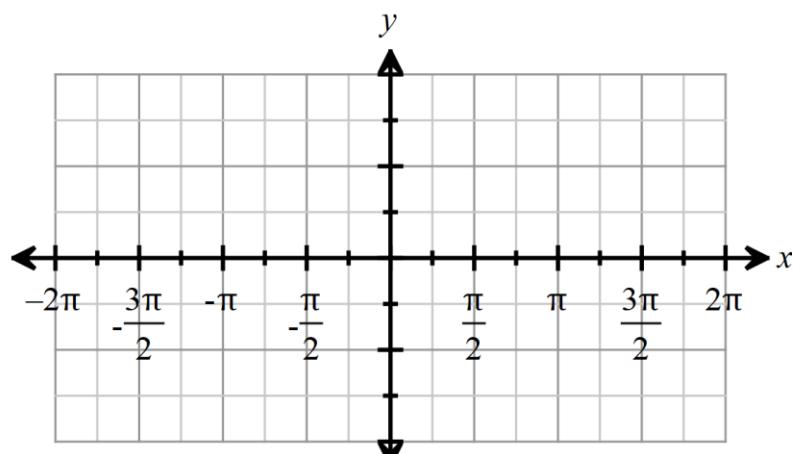
P = _____

D = _____

R: _____

VS: _____

GAP: _____



4) $y = -\cot\left(x - \frac{\pi}{4}\right)$

P = _____

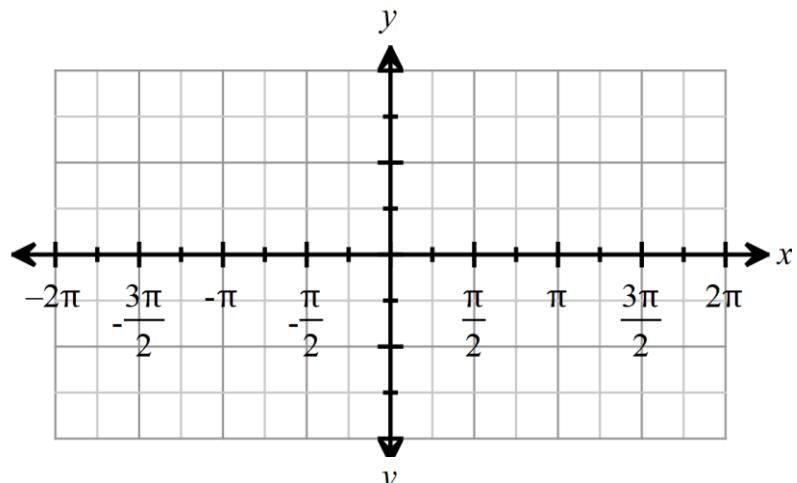
D = _____

R: _____

Phase Shift: _____

GAP: _____

What is another equation for this graph?



5) $y = \cot\left(x + \frac{\pi}{4}\right)$

P = _____

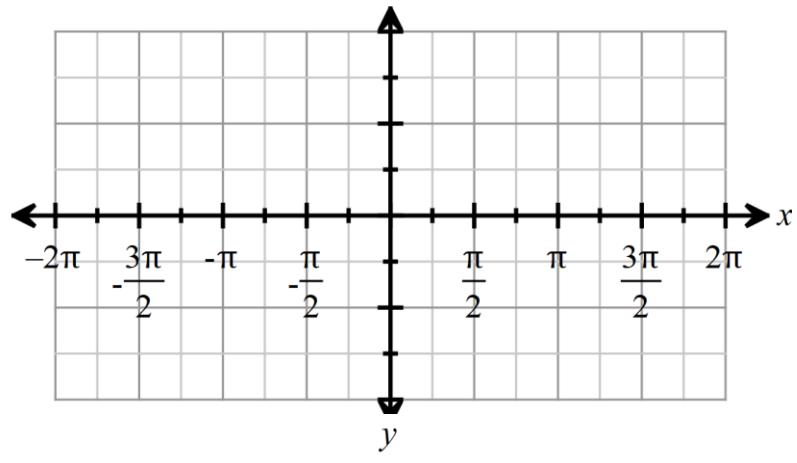
D = _____

R: _____

Phase Shift: _____

GAP: _____

What is another equation for this graph?



6) $y = 2\tan\left(x - \frac{\pi}{2}\right) + 1$

P = _____

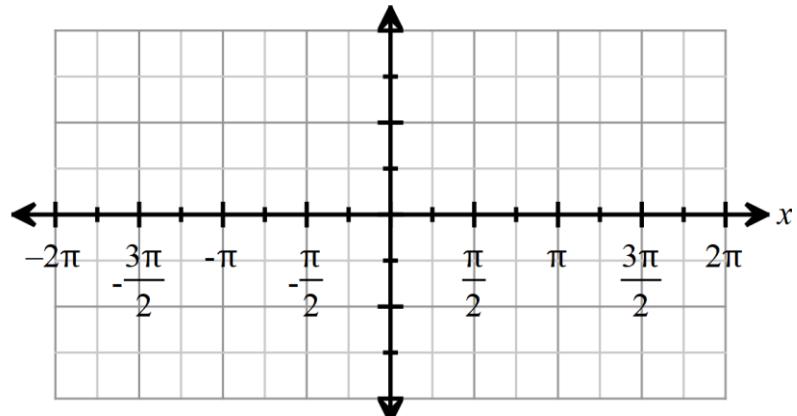
D = _____

R: _____

Phase Shift: _____

GAP: _____

VS: _____



What is another equation for this graph?

Find phase shift of each and state whether the graph is increasing or decreasing.

7) $y = -8\tan(2x - \pi)$

8) $y = 7\cot3\left(x - \frac{\pi}{3}\right)$

9) $y = -\cot\left(4x - \frac{\pi}{16}\right)$

10) $y = 3\tan9(x - \pi)$

11) $y = -\tan\left(3x - \frac{\pi}{4}\right)$

12) $y = 4\cot(4x + 5)$

13) Write an equation for an increasing tangent graph with a period of π and a phase shift $\frac{\pi}{7}$

14) Write an equation for a decreasing cotangent graph with a period of π and a phase shift of $-\frac{2\pi}{9}$

Trig 4.6B Worksheet – Graphing $\tan(x)$ and $\cot(x)$ Stretching and Compressing

Graph the following functions.

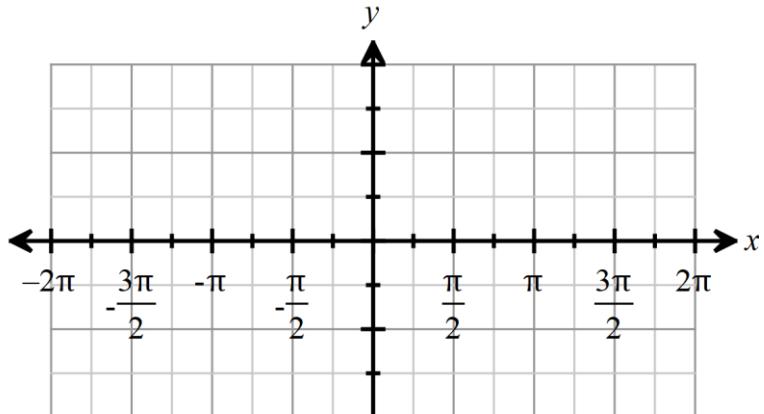
1) $y = 2\tan(2x)$

P = _____

D = _____

R: _____

GAP: _____



2) $y = \cot(3x) + 1$

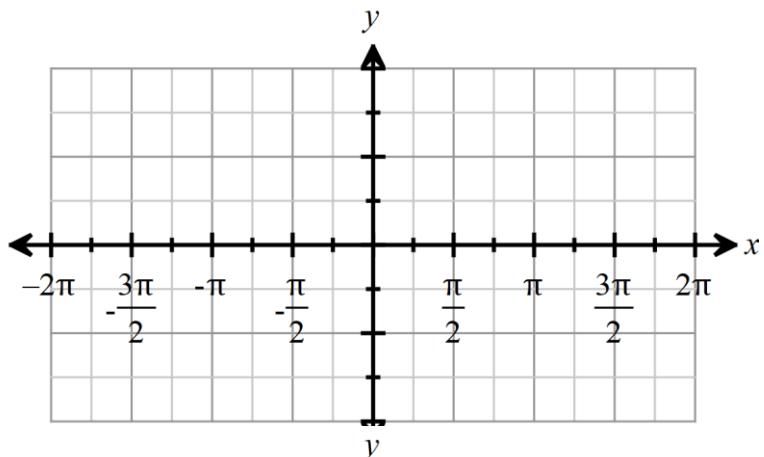
P = _____

D = _____

R: _____

GAP: _____

V.S.: _____



3) $y = -\tan 2(x + \pi)$

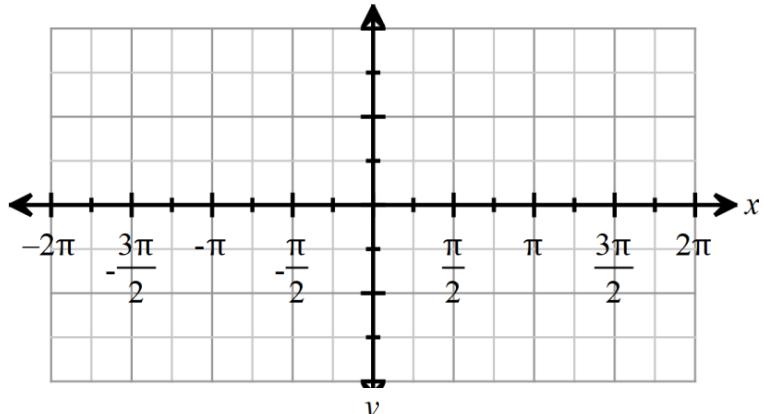
P = _____

D = _____

R: _____

Phase Shift: _____

GAP: _____



4) $y = -\cot 4\left(x - \frac{\pi}{4}\right)$

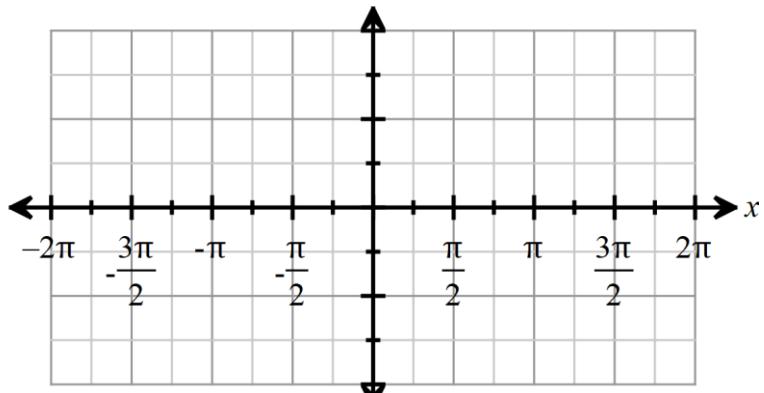
P = _____

D = _____

R: _____

Phase Shift: _____

GAP: _____



What is another equation for this graph?

5) $y = -\cot 2 \left(x + \frac{\pi}{4} \right)$

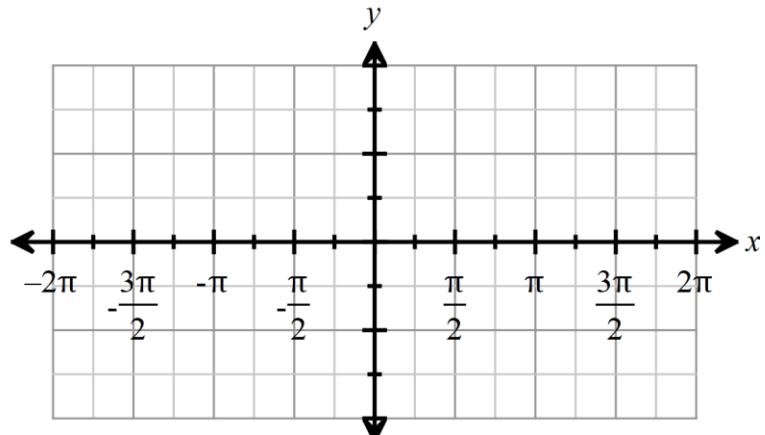
P = _____

D = _____

R: _____

Phase Shift: _____

GAP: _____



What is another equation for this graph?

6) $y = \tan \left(\frac{x}{2} - \frac{5}{8} \right) + 5$

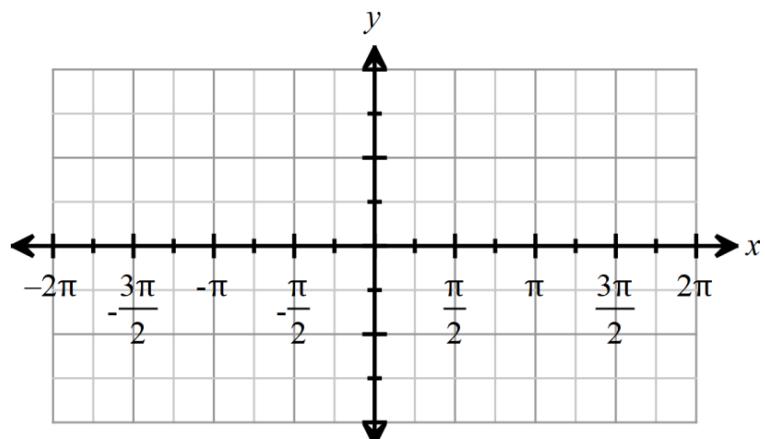
P = _____

D = _____

R: _____

GAP: _____

V.S.: _____



What is another equation for this graph?

Find the period of each.

7) $y = -8\tan(2x - \pi)$

8) $y = 7\cot 3 \left(x - \frac{\pi}{3} \right)$

9) $y = -\cot 4 \left(4x - \frac{\pi}{16} \right)$

10) $y = 3\tan 9(x - \pi)$

11) $y = -\tan \left(3x - \frac{\pi}{4} \right)$

12) $y = 4\cot(4x + 5)$

13) Write an equation for an increasing tangent graph with a period of 4π and a phase shift of $\frac{\pi}{7}$

14) Write an equation for a decreasing cotangent graph with a period of 3π and a phase shift of $\frac{-2\pi}{9}$

Trig 4.6C Worksheet – Graphing All Trig Functions

Graph each and list the important information.

1) $y = -2\tan(2x) - 1$

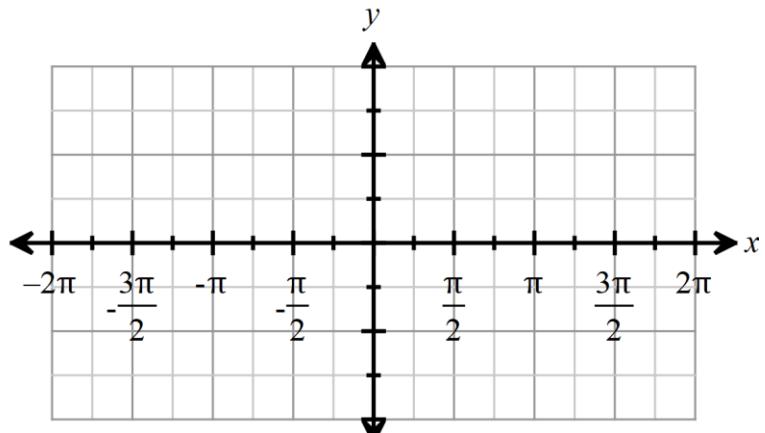
P = _____

D = _____

R: _____

GAP: _____

V.S.: _____



Write a $\cot(x)$ equation for this graph _____

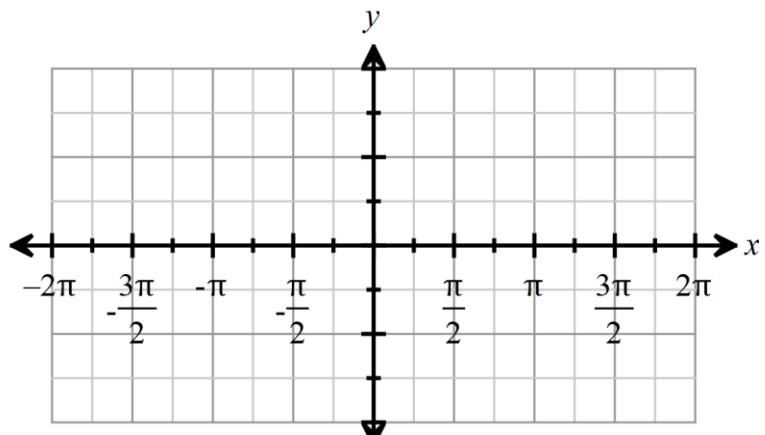
2) $y = 3\cot\left(\frac{x}{4}\right)$

P = _____

D = _____

R: _____

GAP: _____



Write a $\tan(x)$ equation for this graph _____

3) Graph $y = -\sin\left(\frac{1}{2}x - \frac{\pi}{4}\right) + 1$

A = _____

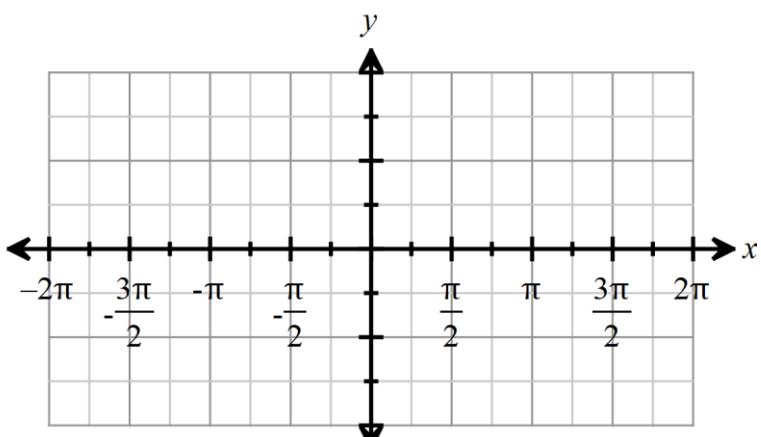
P = _____

D = _____

R = _____

VS: _____

PS: _____



4) $y = 2\cos(2x - \pi)$

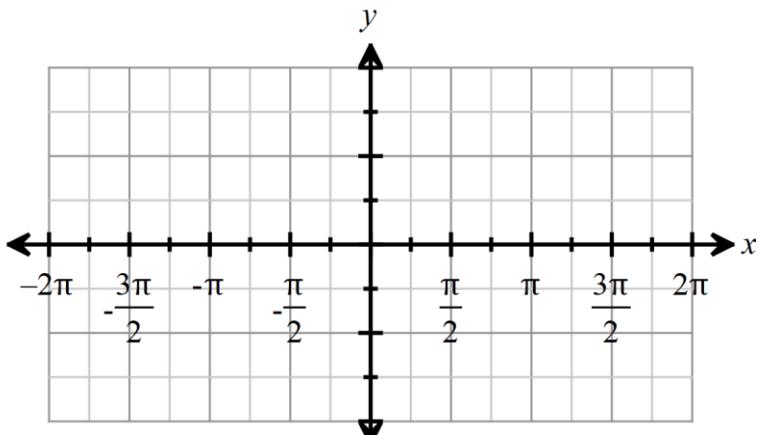
A = _____

P = _____

D = _____

R = _____

PS: _____



GAP: _____

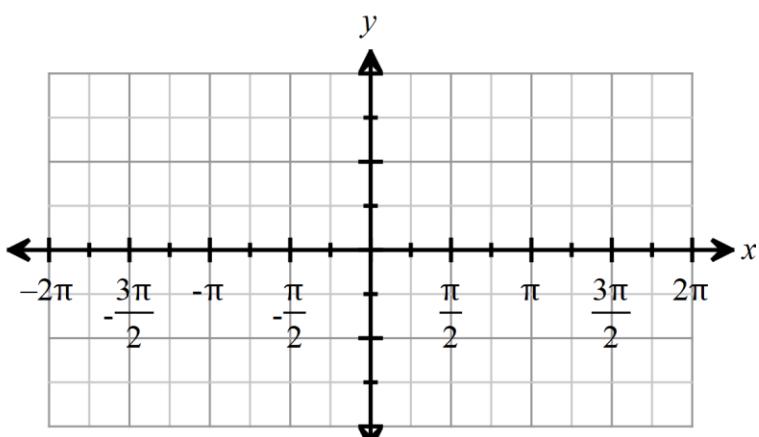
5) $y = -3\csc 2\left(x - \frac{\pi}{4}\right)$

P = _____

D = _____

R: _____

Phase Shift: _____



GAP: _____

What is another equation for this graph?

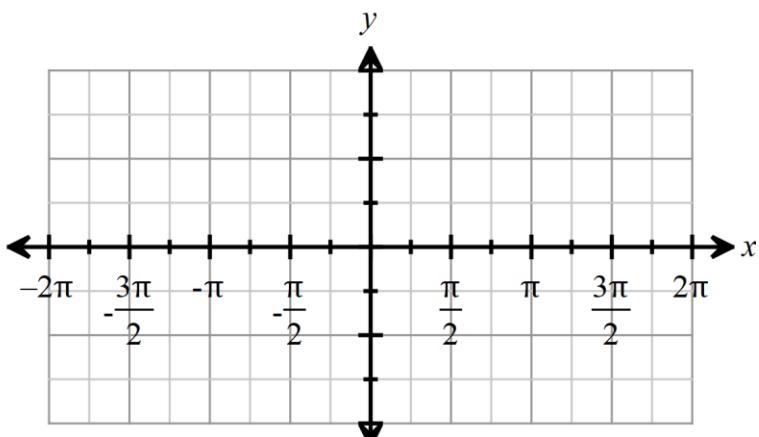
6) $y = -\sec(4x - \pi) - 1$

P = _____

D = _____

R: _____

Phase Shift: _____



GAP: _____

What is another equation for this graph?

- 7) The period of a decreasing $\tan(x)$ graph is 3π with a phase shift of $-\frac{\pi}{6}$. The graph passes through $(\frac{7\pi}{12}, -3)$. Write an equation to represent this situation.

Trig 7B Worksheet – Trig Inverses Worksheet

Find each without a calculator.

$$1) \sin^{-1}(1) + \cos^{-1}(0) - \tan^{-1}(1)$$

$$2) \cos^{-1}(-1) - 2\sin^{-1}\left(-\frac{1}{2}\right) + 3\sin^{-1}\left(\frac{1}{2}\right)$$

$$3) \sec^{-1}(-1) + 15\sin^{-1}(0)$$

$$4) \csc^{-1}(2) + 16\sin^{-1}(-1) - 2\cos^{-1}(-1)$$

$$5) \sin^{-1}\left[\cos\left(\frac{\pi}{6}\right)\right]$$

$$6) \cos^{-1}\left[\tan\left(\frac{\pi}{4}\right)\right]$$

$$7) \sin\left[\cos^{-1}\left(\frac{3}{5}\right)\right]$$

$$8) \tan^{-1}\left[\sin\left(\frac{-\pi}{2}\right)\right] + \cos(0) - 17\sin(0)$$

$$9) \cot\left[\cos^{-1}\left(\frac{12}{13}\right)\right]$$

$$10) \sin[\sin^{-1}(-1)] + \cos[\cos^{-1}(-1)] + \tan[\tan^{-1}(-1)]$$

Use a right triangle to write each expression as an algebraic expression. Assume that x is positive and that the given inverse trig function is defined for the expression in x .

11) $\tan[\cos^{-1}(x)]$

12) $\cos[\sin^{-1}(2x)]$

13) $\cos \left[\sin^{-1} \left(\frac{1}{x} \right) \right]$

14) $\sec \left[\cos^{-1} \left(\frac{1}{x} \right) \right]$

Determine the domain and range of each function.

15) $f(x) = \sin[\sin^{-1}(x)]$

16) $f(x) = \sin^{-1}[\sin(x)]$

17) $f(x) = \cos[\cos^{-1}(x)]$

18) $f(x) = \cos^{-1}[\sin(x)]$