

Trig Polar 6.3B Worksheet
Equation Conversions

Name Key

Date _____

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Write each rectangular equation in polar form.

1) $x^2 + y^2 = 9$

$r = \pm 3$

2) $y = 3$

$r \sin \theta = 3$
 $r = 3 / \sin \theta = 3 \csc \theta$

3) $x = 5$

$r \cos \theta = 5$
 $r = 5 / \cos \theta = 5 \sec \theta$

4) $x^2 - y^2 = 1$

$r \cos \theta - r^2 \sin^2 \theta = 1$

$r^2 = 1 / (\cos^2 \theta - \sin^2 \theta) = 1 / \cos 2\theta$

6)

$3x + y = 7$

5) $x^2 + y^2 - 2y = 0$

$r^2 - 2r \sin \theta = 0$

$r = 2 \sin \theta$

7) $x^2 + y^2 = 16$

8) $(x - 2)^2 + y^2 = 4$

$3r \cos \theta + r \sin \theta = 7$

$r = \pm 4$

$x^2 - 4x + 4 + y^2 = 4$

$r(3 \cos \theta + \sin \theta) = 7$

$x^2 + y^2 - 4x = 0$

$r = 7 / (3 \cos \theta + \sin \theta)$

$r^2 - 4r \cos \theta = 0$
 $r - 4 \cos \theta = 0$
 $r = 4 \cos \theta$

9) $y^2 = 6x$

10) $y = 2x$

11) $y = -x$

$r^2 \sin^2 \theta = 6r \cos \theta$

$r \sin^2 \theta = 6 \cos \theta$

$r = 6 \cos \theta / \sin^2 \theta$

$\theta = \tan^{-1}(2)$

$\theta = 63^\circ \text{ or } 1.1$

$\theta = 7\pi/4 \text{ or } -\frac{\pi}{4}$

Write each polar equation in rectangular form.

12) $r = 16$

13) $\theta = \pi/3$

14) $r \cos \theta = 5$

$x^2 + y^2 = 256$

$y = \sqrt{3}x$

$x = 5$

15) $r \sin \theta = 17$

16) $r = 3 \sec \theta$

17) $r = -8 \csc \theta$

$y = 17$

$r \cos \theta = 3$

$x = 3$

$r \sin \theta = -8$

$y = -8$

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18) $\theta = \pi/7$

$$y = .48x$$

19) $r = \sin\theta$

$$\begin{aligned} r^2 &= rs\sin\theta \\ x^2 + y^2 &= y \end{aligned}$$

20) $r = \cos\theta$

$$\begin{aligned} r^2 &= r\cos\theta \\ x^2 + y^2 &= x \end{aligned}$$

21) $r = 12\cos\theta$

$$r^2 = 12rcos\theta$$

$$x^2 + y^2 = 12x$$

22) $r = 6\cos\theta + 4\sin\theta$

$$r^2 = 6r\cos\theta + 4r\sin\theta$$

$$x^2 + y^2 = 6x + 4y$$

23) $r = 8\cos\theta + 2\sin\theta$

$$r^2 = 8r\cos\theta + 2r\sin\theta$$

$$x^2 + y^2 = 8x + 2y$$

24) $r^2\sin 2\theta = 2$

$$r^2(2\sin\theta\cos\theta) = 2$$

$$rsin\theta rcos\theta = 1$$

$$yx = 1$$

$$xy = 1$$

or

$$y = \frac{1}{x}$$

25) $\theta = 72^\circ$

$$y = \tan 72^\circ x$$

$$y = 3.08x$$