

Trig Complex Numbers in Polar Form 6.5 Worksheet

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In exercises 1-8 plot each complex number. Then write the complex numbers in polar form. You may express the argument (angle) in degrees or radians.

1.  $2 - 2i$

$$2\sqrt{2} \left( \cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4} \right)$$

2.  $-1 - i$

$$\sqrt{2} \left( \cos \frac{5\pi}{4} + i \sin \frac{5\pi}{4} \right)$$

3.  $-4i$

$$4 \left( \cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2} \right)$$

4.  $2\sqrt{3} - 2i$

$$4 \left( \cos \frac{11\pi}{6} + i \sin \frac{11\pi}{6} \right)$$

5.  $-3$

$$3 \left( \cos \pi + i \sin \pi \right)$$

6.  $-3\sqrt{2} - 3i\sqrt{3}$

$$3\sqrt{5} \left( \cos 4.3 + i \sin 4.3 \right)$$

7.  $-3 + 4i$

8.  $3 - i\sqrt{3}$

$$5 \left( \cos 2.2 + i \sin 2.2 \right)$$

$$2\sqrt{3} \cos \frac{11\pi}{6} +$$

$$2.2 \approx 126.9^\circ$$

$$i \sin \frac{11\pi}{6}$$

In exercise 9-14 write each complex number in rectangular form. If necessary, round to the nearest tenth.

9.  $6(\cos 30^\circ + i \sin 30^\circ)$

$$3\sqrt{3} + 3i$$

10.  $4(\cos 240^\circ + i \sin 240^\circ)$

$$-2 - 2\sqrt{3}i$$

11.  $8 \left( \cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4} \right)$

12.  $8 \left( \cos \frac{5\pi}{3} + i \sin \frac{5\pi}{3} \right)$

$$4\sqrt{2} - 4\sqrt{2}i$$

$$4 - 4\sqrt{3}i$$

13.  $20 (\cos 205^\circ + i \sin 205^\circ)$

$$-18.1 - 8.5i$$

14.  $14(\cos -10^\circ + i \sin -10^\circ)$

$$13.8 - 2.4i$$

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In exercise 15-18, find the product ( $z_1 z_2$ ) of the complex numbers. Leave answers in polar form.

15.  $z_1 = 6 (\cos 20^\circ + i \sin 20^\circ)$

$$z_2 = 13(\cos 50^\circ + i \sin 50^\circ)$$

$$78 \text{cis } 70^\circ$$

16.  $z_1 = 4 (\cos 15^\circ + i \sin 15^\circ)$

$$z_2 = 13(\cos -50^\circ + i \sin -50^\circ)$$

$$52 \text{cis } 325^\circ$$

17.  $z_1 = 3 (\cos \frac{5\pi}{8} + i \sin \frac{5\pi}{8})$

$$z_2 = 10 (\cos \frac{\pi}{16} + i \sin \frac{\pi}{16})$$

18.  $z_1 = \cos \frac{\pi}{4} + i \sin \frac{\pi}{4}$

$$z_2 = \cos \frac{\pi}{3} + i \sin \frac{\pi}{3}$$

$$30 \text{cis } \frac{11\pi}{16}$$

$$\text{cis } \frac{7\pi}{12}$$

In exercise 19-22 find the quotient  $z_1/z_2$  of the complex numbers. Leave answers in polar form. Express the argument as an angle between  $0^\circ$  and  $360^\circ$  or between  $0$  and  $2\pi$ .

19.  $z_1 = 20 (\cos 75^\circ + i \sin 75^\circ)$

$$z_2 = 4 (\cos 25^\circ + i \sin 25^\circ)$$

$$5 \text{cis } 50^\circ$$

20.  $z_1 = 50 (\cos 80^\circ + i \sin 80^\circ)$

$$z_2 = 10 (\cos 20^\circ + i \sin 20^\circ)$$

$$5 \text{cis } 60^\circ$$

21.  $z_1 = 3(\cos \frac{\pi}{5} + i \sin \frac{\pi}{5})$

$$z_2 = 33(\cos \frac{\pi}{20} + i \sin \frac{\pi}{20})$$

$$\frac{1}{11} \text{cis } \frac{3\pi}{20}$$

22.  $z_1 = 13(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6})$

$$z_2 = 26(\cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6})$$

$$\frac{1}{2} \text{cis } \frac{4\pi}{3}$$