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In exercise 1, find all the complex roots. Write roots in polar form and in rectangular with the argument as an angle between 0 and 360° . (3 points)

1) Find the complex cube roots of $64(\cos 210^\circ + i \sin 210^\circ)$

Polar Form:

$$\begin{aligned} 4\text{cis} 70^\circ \\ 4\text{cis} 190^\circ \\ 4\text{cis} 310^\circ \end{aligned}$$

Rectangular Form: Use Calculator

$$1.37 + 3.76i \quad -3.94 - 6.9i \quad 2.57 - 3.06i$$

In exercise 2, find all the complex roots. Write roots in polar form and in rectangular with the argument as an angle between 0 and 2π . (4 points)

2) Find the complex fourth roots of $81(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3})$.

Polar Form:

$$\begin{aligned} 3\text{cis} \pi/2 \\ 3\text{cis} 7\pi/12 \\ 3\text{cis} 13\pi/12 \\ 3\text{cis} 19\pi/12 \end{aligned}$$

Rectangular Form: Use Calculator

$$\begin{aligned} 2.90 + 0.78i & \quad -0.78 + 2.90i & \quad -2.90 - 0.78i \\ 0.78 - 2.90i & & \end{aligned}$$

Solve each under the set of complex numbers. Write your answers in polar and rectangular form. Store your solutions under x and check each answer. (5 points each)

3) $x^3 = 8$

$$2cis0 = 2$$

$$2cis\frac{2\pi}{3} = -1 + \sqrt{3}i$$

$$2cis\frac{4\pi}{3} = -1 - \sqrt{3}i$$

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* 4) $x^4 = -16$

$$x^4 = 16cis\pi$$

$$x_1 = (16cis\pi)^{1/4}$$

$$x_1 = 2cis\pi/4 = \sqrt{2} + \sqrt{2}i$$

$$x_2 = 2cis3\pi/4 = -\sqrt{2} + \sqrt{2}i$$

$$x_3 = 2cis5\pi/4 = -\sqrt{2} - \sqrt{2}i$$

$$x_4 = 2cis\frac{7\pi}{4} = \sqrt{2} - \sqrt{2}i$$

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